



33rd Austrian Mathematical Olympiad

Beginner's Competition

June 13, 2002

1. We calculate the sum of 7 consecutive even natural numbers (e.g., $2 + 4 + 6 + 8 + 10 + 12 + 14$) and call it A , then the sum of the following 7 even numbers (here $16 + 18 + \dots$) and call it B and finally again the sum of the following 7 even numbers and call it C .

Can their product be $ABC = 2002^3$?

2. Show that no positive real number x exists such that

$$x^{\lfloor x \rfloor} = \frac{9}{2}.$$

3. Determine all real numbers x that satisfy the following inequality.

$$|x^2 - 4x + 1| > |x^2 - 4x + 5|.$$

4. In a trapezoid $ABCD$ with base AB let E be the midpoint of the side AD . Further assume that $2\overline{CD} = \overline{EC} = \overline{BC} = b$. Let the angle ECB be 120° .

Construct the trapezoid and determine its area as a function of b .